INSTITUTE OF COST AND MANAGEMENT ACCOUNTANTS OF PAKISTAN



Fall 2012 (February 2013) Examinations

Wednesday, the 27th February 2013

BUSINESS MATHEMATICS & STATISTICAL INFERENCE – (ML-202) SEMESTER-2

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- (i) Attempt ALL questions.
- (ii) Answers must be neat, relevant and brief.
- (iii) In marking the question paper, the examiners take into account clarity of exposition, logic of arguments, effective presentation, language and use of clear diagram / chart, where appropriate.
- (iv) Read the instructions printed inside the top cover of answer script CAREFULLY before attempting the paper.
- (v) Use of non-programmable scientific calculators of any model is allowed.
- (vi) DO NOT write your Name, Reg. No. or Roll No. anywhere inside the answer script.
- (vii) Question No.1 "Multiple Choice Question" printed separately, is an integral part of this question paper.
- (viii) Question Paper must be returned to invigilator before leaving the examination hall.
- **Q.2 (a)** Simplify the following:

$$\frac{\sqrt{x^{3}y^{5}}}{\sqrt[4]{x^{7}y^{2}}} \times \frac{\sqrt{xy^{3}}}{\sqrt[4]{xy^{6}}}$$

SECTION "A"

(b) Solve the following equation:

$$\frac{x+6}{5} - \frac{2x-1}{2} = 3$$

- (c) An investor has Rs.400,000 to invest. Three investment opportunities are being considered, which have expected annual interest rates of 10%, 7%, and 8%. A goal has been set to earn an annual income of Rs.32,000 on the total investments. One condition set by the trust is that the combined investment in alternative 2 and 3 should be three times the amount invested in alternative 1. Determine whether there is a meaningful investment strategy, which will satisfy this requirement.
- **Q.3** (a) Find the location of all the critical points:

$$f(x) = x^2 + 5x + 6$$

(b) How much money must be deposited at the end of each quarter if the objective is to accumulate Rs.600,000 after 8 years? Assume interest is earned at the rate of 10 percent per year compounded quarterly.

Given that
$$S_n = R \{(1 + i)^n - 1\} \div i$$
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(c) Find the derivative of the following function:

$$f(x) = \frac{6x^2 + 3x - 5}{\ln(5x^2 + 4)}$$

(d) A sum of Rs.200,000 is to grow to Rs.1,000,000 over an 8-year period. At what annual interest rate must it be invested, given that the interest is compounded quarterly?

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SECTION "B"

- **Q.4 (a)** Random samples of size 2 are drawn from the finite population 2, 4, 6, 8, and 10 without replacement. Construct sampling distribution of mean.
 - (b) The following scores represent the marks of 39 students:

| 25 | 20 | 35 | 45 | 14 | 25 | 32 | 17 | 28 | 23 | 18 | 31 | 37 |
|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 10 | 19 | 30 | 33 | 21 | 22 | 41 | 34 | 29 | 27 | 44 | 23 | 12 |
| 44 | 12 | 40 | 22 | 25 | 37 | 28 | 37 | 19 | 40 | 12 | 39 | 25 |

Required:

Set up a frequency distribution for the above data.

(c) Following are the marks obtained by 100 candidates in a Statistics examination:

| Marks obtained | 10 – 24 | 25 – 39 | 40 – 54 | 55 – 69 | 70 – 84 | 85 – 99 |
|-----------------|---------|---------|---------|---------|---------|---------|
| No. of students | 10 | 16 | 23 | 29 | 16 | 6 |

Required:

Calculate arithmetic mean and median.

- (d) Population mean and variance of 10 observations are 15 and 50 respectively. One observation (which is 12) is replaced by 18. Find new mean and variance.
- **Q.5** (a) A study was made by a retail merchant to determine the relation between weekly advertising expenditure and sales. Following data was recorded:

| Advertising Cost (Rs. '000') | 48 | 22 | 25 | 20 | 30 | 50 | 40 | 55 | 45 |
|------------------------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| Sales (Rs. '000') | 380 | 420 | 395 | 365 | 475 | 440 | 490 | 565 | 515 |

Required:

- (i) Find the equation of the regression line.
- (ii) Predict the amount of sales if advertising expenditure is Rs.60,000.
- (b) Find Fisher's Ideal index number of the year 2007 (treating 2012 as base year) for the following data:

| Commodity | Price | (Rs.) | Quantity (Units) | | | |
|-----------|-------|--------|------------------|------|--|--|
| Commonly | 2007 | 2012 | 2007 | 2012 | | |
| Α | 12.50 | 15.00 | 125 | 150 | | |
| В | 30.00 | 40.00 | 160 | 185 | | |
| С | 75.00 | 85.10 | 140 | 165 | | |
| D | 95.15 | 105.00 | 78 | 85 | | |

- (c) The weights of 10 boxes of a certain brand of cereal have a mean content of 278 grams with a standard deviation of 9.64 grams. If these boxes were purchased from 10 different stores and average price per box is Rs.129 with a standard deviation of Rs.9, can you conclude that the weights are relatively more homogeneous than the prices?
- **Q.6** (a) Describe the various characteristics of 'moving averages'.
 - (b) In a poker hand consisting of 5 cards, find the probability of holding at most 2 aces. 06
 - (c) A random sample of 17 college students showed mean marks 50 and variance 36. Assuming the scores to be normally distributed, construct a 95% confidence interval for average marks scored by the entire students? ($t_{0.05,16} = 1.746$ or $t_{0.025,16} = 2.120$) 06

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