# INSTITUTE OF COST AND MANAGEMENT ACCOUNTANTS OF PAKISTAN 

## Fall 2012 (February 2013) Examinations

Wednesday, the 27th February 2013

# BUSINESS MATHEMATICS \& STATISTICAL INFERENCE - (ML-202) SEMESTER-2 

Time Allowed: 02 Hours 45 Minutes
Maximum Marks: 90
Roll No.:
(i) Attempt ALL questions.
(ii) Answers must be neat, relevant and brief.
(iii) In marking the question paper, the examiners take into account clarity of exposition, logic of arguments, effective presentation, language and use of clear diagram / chart, where appropriate.
(iv) Read the instructions printed inside the top cover of answer script CAREFULLY before attempting the paper.
(v) Use of non-programmable scientific calculators of any model is allowed.
(vi) DO NOT write your Name, Reg. No. or Roll No. anywhere inside the answer script.
(vii) Question No. 1 - "Multiple Choice Question" printed separately, is an integral part of this question paper.
(viii) Question Paper must be returned to invigilator before leaving the examination hall.

## SECTION "A"

Q. 2 (a) Simplify the following:

05

$$
\frac{\sqrt{x^{3} y^{5}}}{\sqrt[4]{x^{7} y^{2}}} \times \frac{\sqrt{x y^{3}}}{\sqrt[4]{x y^{6}}}
$$

(b) Solve the following equation:

$$
\frac{x+6}{5}-\frac{2 x-1}{2}=3
$$

(c) An investor has Rs. 400,000 to invest. Three investment opportunities are being considered, which have expected annual interest rates of $10 \%, 7 \%$, and $8 \%$. A goal has been set to earn an annual income of Rs.32,000 on the total investments. One condition set by the trust is that the combined investment in alternative 2 and 3 should be three times the amount invested in alternative 1. Determine whether there is a meaningful investment strategy, which will satisfy this requirement.
Q. 3 (a) Find the location of all the critical points:

$$
f(x)=x^{2}+5 x+6
$$

(b) How much money must be deposited at the end of each quarter if the objective is to accumulate Rs.600,000 after 8 years? Assume interest is earned at the rate of 10 percent per year compounded quarterly.
Given that $S_{n}=R\left\{(1+i)^{n}-1\right\} \div i$
(c) Find the derivative of the following function:

$$
f(x)=\frac{6 x^{2}+3 x-5}{\ln \left(5 x^{2}+4\right)}
$$

(d) A sum of Rs.200,000 is to grow to Rs.1,000,000 over an 8 -year period. At what annual interest rate must it be invested, given that the interest is compounded quarterly?
Q. 4 (a) Random samples of size 2 are drawn from the finite population 2, 4, 6, 8, and 10 without replacement. Construct sampling distribution of mean.
(b) The following scores represent the marks of 39 students:

| 25 | 20 | 35 | 45 | 14 | 25 | 32 | 17 | 28 | 23 | 18 | 31 | 37 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 10 | 19 | 30 | 33 | 21 | 22 | 41 | 34 | 29 | 27 | 44 | 23 | 12 |
| 44 | 12 | 40 | 22 | 25 | 37 | 28 | 37 | 19 | 40 | 12 | 39 | 25 |

## Required:

Set up a frequency distribution for the above data.
(c) Following are the marks obtained by 100 candidates in a Statistics examination:

| Marks obtained | $10-24$ | $25-39$ | $40-54$ | $55-69$ | $70-84$ | $85-99$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 10 | 16 | 23 | 29 | 16 | 6 |

## Required:

Calculate arithmetic mean and median.
(d) Population mean and variance of 10 observations are 15 and 50 respectively. One observation (which is 12 ) is replaced by 18 . Find new mean and variance.
Q. 5 (a) A study was made by a retail merchant to determine the relation between weekly advertising expenditure and sales. Following data was recorded:

| Advertising Cost (Rs. '000') | 48 | 22 | 25 | 20 | 30 | 50 | 40 | 55 | 45 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Sales (Rs. '000') | 380 | 420 | 395 | 365 | 475 | 440 | 490 | 565 | 515 |

## Required:

(i) Find the equation of the regression line.
(ii) Predict the amount of sales if advertising expenditure is Rs.60,000.
(b) Find Fisher's Ideal index number of the year 2007 (treating 2012 as base year) for the following data:

| Commodity | Price (Rs.) |  | Quantity (Units) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{2 0 0 7}$ | $\mathbf{2 0 1 2}$ | $\mathbf{2 0 0 7}$ | $\mathbf{2 0 1 2}$ |
| A | 12.50 | 15.00 | 125 | 150 |
| B | 30.00 | 40.00 | 160 | 185 |
| C | 75.00 | 85.10 | 140 | 165 |
| D | 95.15 | 105.00 | 78 | 85 |

(c) The weights of 10 boxes of a certain brand of cereal have a mean content of 278 grams with a standard deviation of 9.64 grams. If these boxes were purchased from 10 different stores and average price per box is Rs. 129 with a standard deviation of Rs.9, can you conclude that the weights are relatively more homogeneous than the prices?
Q. 6 (a) Describe the various characteristics of 'moving averages'.
(b) In a poker hand consisting of 5 cards, find the probability of holding at most 2 aces.
(c) A random sample of 17 college students showed mean marks 50 and variance 36 Assuming the scores to be normally distributed, construct a $95 \%$ confidence interval for average marks scored by the entire students? $\left(\mathrm{t}_{0.05,16}=1.746\right.$ or $\mathrm{t}_{0.025,16}=2.120$ )

