# INSTITUTE OF COST AND MANAGEMENT ACCOUNTANTS OF PAKISTAN



## Winter (November) 2011 Examinations

Saturday, the 19th November 2011

### BUSINESS MATHEMATICS & STATISTICS - (S-203) STAGE - 2

| Time   | Allo                             | wed: 02 Hours 45 Minutes  | Maximum Marks:  | 80 Roll No.:   |  |  |  |  |  |
|--------|----------------------------------|---|---|--|--|--|--|--|--|
| (i)    | Atte                             | mpt ALL questions.  |   |  |  |  |  |  |  |
| (ii)   | Ansv                             | nswers must be neat, relevant and brief.  |   |  |  |  |  |  |  |
| (iii)  | In m<br>effec                    | arking the question paper, the examin<br>ctive presentation, language and use c   | ers take into account clar<br>of clear diagram / chart, w | ity of exposition, logic here appropriate.                       | of arguments,  |  |  |  |  |
| (iv)   | Read                             | ead the instructions printed inside the top cover of answer script CAREFULLY before attempting the paper.   |   |  |  |  |  |  |  |
| (v)    | Use                              | of non-programmable scientific calcul   | ators of any model is allow                               | wed.   |  |  |  |  |  |
| (vi)   | DO I                             | NOT write your Name, Reg. No. or Ro   | II No. anywhere inside the                                | e answer script.   |  |  |  |  |  |
| (vii)  | Que                              | stion No.1 – "Multiple Choice Question  | n" printed separately, is ar                              | n integral part of this q  | uestion paper.   |  |  |  |  |
| (viii) | Que                              | stion Paper must be returned to inv   | rigilator before leaving t                                | he examination hall.   |  |  |  |  |  |
|        |                                  |   | SECTION "A"   |  | Marks  |  |  |  |  |
| Q. 2   | (a)                              | A firm sells a single product for R<br>materials and Rs.40 for the labor.<br>function stated in terms of x, th<br>earned if annual sales are 50,000   | Annual fixed costs are<br>e number of units pro<br>units? | e costs per unit are<br>Rs.250,000. Constr<br>oduced and sold. W | Rs.30 for the <b>08</b><br>ruct the profit<br>/hat profit is |  |  |  |  |
|        | (b)                              | Solve the quadratic equation by fa  | actorization $2x^2 - x - 1$                               | = 0  | 04   |  |  |  |  |
|        | (c)                              | Solve the following system of equ<br>$3x_2 + x_3 = 30$<br>$x_1 + x_2 = 15$<br>$2x_1 + 3x_2 + 3x_3 = 56$   | ations by Gaussian Elir                                   | mination Method:   | 08   |  |  |  |  |
| Q. 3   | (a)                              | The function describing the margi $MC = 6x$   | nal cost (in rupees) of p<br>: + 2,000                    | producing a product  | is: 06   |  |  |  |  |
|        |                                  | Where 'x' equals the number of Rs.200,000 when 100 units are p  | of units produced. It is roduced. Determine the           | s known that total<br>total cost function.                       | cost equals  |  |  |  |  |
|        | (b)                              | Determine the following definite Ir   | ntegral:  |  | 06   |  |  |  |  |
|        |                                  | $\int_{2}^{4} \frac{2x-1}{2x^2-2x+5}  \mathrm{d}x$  |   |  |  |  |  |  |  |
|        | (c)                              | (c) The annual profit for a firm depends upon the number of units produced. Specially, the function which describes the relationship between profit P (stated in rupees) and the number of units produced 'x' is: |   |  |  |  |  |  |  |
|        | $P = -0.02x^2 + 2,500x - 40,000$ |   |   |  |  |  |  |  |  |
| Requ   | ired·                            |   |   |  |  |  |  |  |  |
| nequ   | n cu.                            | (i) Determine the number of unit  | ts 'x' which will result in                               | maximum profit.  | 06   |  |  |  |  |
|        |                                  | (ii) What is the expected maximu  | um profit?  | •  | 02   |  |  |  |  |

01

02

02

05

#### **SECTION "B"**

**Q. 4 (a)** Use the method of the least squares to find the regression equation of y on x for the data **05** in the following table:

| Х | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|---|---|---|---|---|---|---|---|
| Y | 2 | 3 | 3 | 4 | 5 | 7 | 8 |

(b) In a factory, item 'A' is being produced by 3 workers. Following are the details of the number of items produced in a day:

| Quality   | Units P | Total |    |       |
|-----------|---------|-------|----|-------|
| Quality   | 1       | 2     | 3  | TOLAI |
| Good      | 70      | 82    | 76 | 228   |
| Defective | 5       | 3     | 4  | 12    |
| Total     | 75      | 85    | 80 | 240   |

### **Required:**

- If one item is selected at random what is the probability that:
- (i) it is defective?
- (ii) it is defective or produced by Worker-1?
- (iii) it is of good quality or was produced by Worker-2?
- **Q.5** (a) The performance of the two players is given below:

| Player X (No. of runs) (x)    | 24 | 39 | 54 | 15 | 27 | 19 | 25 | 37 | 8 | 11 |
|-------------------------------|----|----|----|----|----|----|----|----|---|----|
| Player Y (No. of wickets) (y) | 3  | 4  | 2  | 5  | 1  | 6  | 8  | 0  | 4 | 9  |

The performance of which player is more consistent?

(b) A poultry packing machine is supposed to put 500 grams of poultry in a container. The packing machine operates with a standard deviation of 25 grams. A random sample of 64 containers was taken to determine whether the machine was working properly. It resulted in the sample mean of 495 grams. Do you think that the machine is required to be repaired? (Use 0.05 level of significance, z<sub>tab</sub> at 0.05 level of significance is 1.96)

### **SECTION "C"**

**Q.6** Following is the data relating to the Project 'X':

| Activity | Preceded by | Elapsed Time (Weeks) |
|----------|-------------|----------------------|
| А        | -           | 2                    |
| В        | Α           | 5                    |
| С        | —           | 2                    |
| D        | B, C        | 4                    |
| Е        | —           | 3                    |
| F        | D, E        | 4                    |
| G        | F           | 5                    |

### **Required:**

- (a) Draw the network diagram of the above project incorporating therein the Earliest Starting 07 Time (EST) and Latest Starting Time (LST) for each activity.
- (b) Compute the total float for each activity.
- **Q.7** Solve the following linear programming model by using simplex method:

| Maximize Z = | 3x1 +              | 2x <sub>2</sub> + | 5x <sub>3</sub>         |     |
|--------------|--------------------|-------------------|-------------------------|-----|
| Subject to   | <b>X</b> 1 +       | 2x <sub>2</sub> + | <b>x</b> <sub>3</sub> ≤ | 500 |
|              | 3x1 +              | +                 | 2x <sub>3</sub> ≤       | 460 |
|              | X <sub>1</sub> +   | 4x <sub>2</sub>   | ≤                       | 420 |
|              | x <sub>1</sub> , x | 2,X <sub>3</sub>  | ≥                       | 0   |

#### THE END

03

10